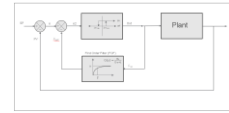


Simple On-Off Control for First Order Systems

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Tools & prerequisites

Software:

- Studio 5000 Logix Designer v35.
- FactoryTalk View ME v12.00.00.

Hardware:

- ControlLogix Logix (1756-L83) FW v35.
- CompactLogix I/O Adapter (5069-AEN2TR).
- CompactLogix Universal Analog Input Card (5069-IY4).
- CompactLogix 16 24VDC output card (5069-OB16F).
- PanelView Plus 7 Performance 700 (2711P-T7C22A9P).

Test System Components:

- 1 Pc 8 liters aquarium.
- 1 pc RTD PT100 Temperature Sensor.
- 1 pc Solid State Relay 24 VDC input coil / 125 VAC output.
- 1 pc 400 watts heating resistor.
-

Files:

- BB.acd Logix Designer Addon Instruction
-

Objective of this document

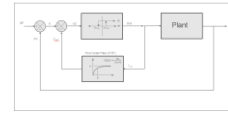
The objective of this document is to present an easy to program and calibrate first order plant control when output of the system is on-off actuator. This algorithm is based on Bang-Bang Control which uses hysteresis to turn on and off the output of the control with an enhancement of a first order filter in an inner feedback loop to increase modulation of the output.

The type of outputs that this control may drive are:

- Solenoid Valves.
- Motorized Valves with 2 positions (Open/Close).
- 1. Solid State Relays (To drive heating resistors).
- 2. Electromechanical Contactors.

This algorithm can replace a Proportional-Integral control loop that needs to be connected to a time proportional output, it is simpler to tune and has less parameters to setup.

Definition of a First Order and Second Order Critically Damped or Overdamped System.



We do not pretend to demonstrate the full control theory of the system nor demonstrate the mathematics behind the implementation of the system, but explain how to program, apply, and calibrate the system. But it is important to identify the system where the algorithm is applicable.

First Order System:

A first order system or plant is one which behavior is determined by a first order differential equation in the form of:

$$\frac{dy(t)}{dt} + a_0y(t) = box(t)$$

Where $y(t)$ is the system output, $x(t)$ is the system input, a_0 is the initial value of the system at $t=0$, K is the system gain (Normally 1 or less than 1).

This equation is better represented in the form of transfer function in LaPlace form as:

$$\frac{Y(s)}{X(s)} = G(s) = \frac{K}{Ts + 1}$$

- K System Gain (b_0/a_0)
- T Time Constant (Related to system capacitance and resistance)

The response of the first order system to a step input of $X(s)=2$ with $T=1$ is shown in Figure 1.

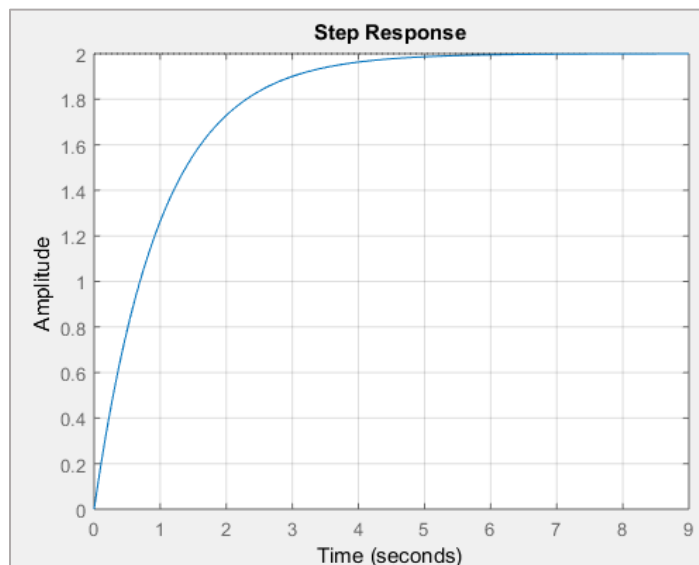


Figure 1. Response of a first order system to a step of magnitude 2

Is well known that the first order system have a define time constant T (Tao) that defines the time where the system output $y(t)$ reaches or trends to reach the input $x(t)$. These values are shown in Figure 2.

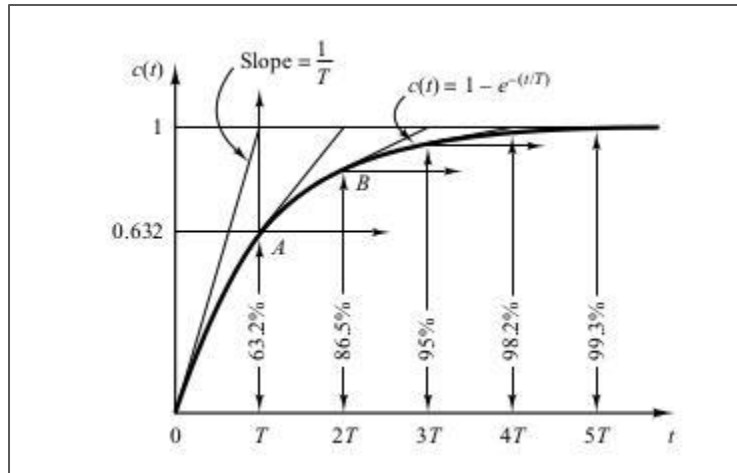
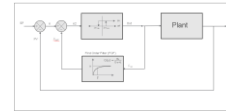


Figure 2. Time response of a first order system

Examples of first order systems:

3. A Resistor and Capacitor circuit.
4. A Height of a tank with inlet flow and outlet flow.
5. The pressure of a tank with inlet flow and outlet flow.
6. Temperature system when heating or cooling.

Second Order Systems

A second order system is defined by a second order differential equation as follows:

$$\tau^2 \cdot \frac{d^2y(t)}{dt^2} + 2\zeta\tau \cdot \frac{dy(t)}{dt} + y(t) = K \cdot x(t)$$

τ : Time Constant (Related to system capacitance and resistance)
 ζ : Damping factor constant
 K : System Gain
 $y(t)$: Output of the system (Behavior)
 $x(t)$: Input of the system

Analogous to the first order system, the transfer function represented in Laplace form is:

$$\frac{Y(s)}{X(s)} = G(s) = \frac{K}{\tau^2 \cdot s^2 + 2\zeta\tau \cdot s + 1}$$

Again, the state response of the system to a state input $x(t(0^-))=0$ and $x(t(0^+)) = C$

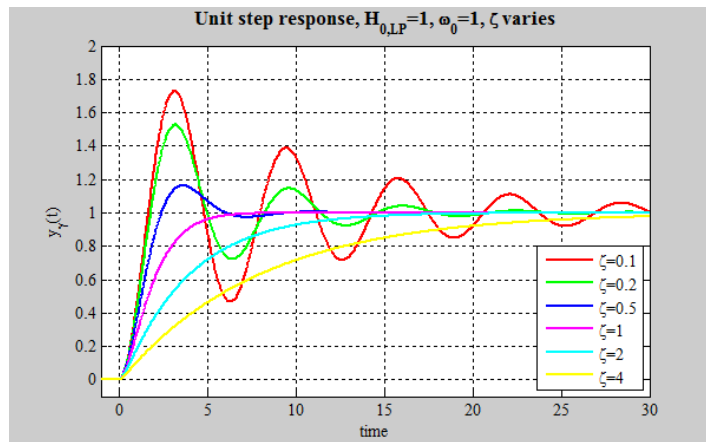
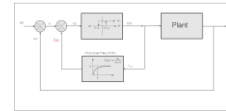


Figure 3. Second Order response to unitary step.

If we observe the graphic, we can define the system behavior in 3 types:

- 7. **Undamped:** When $0 < \zeta < 1$, The system has overshoot and decreased oscillations.
- 8. **Critically Damped:** $\zeta = 1$, The system does not have overshoot nor oscillations.
- 9. **Overdamped:** $\zeta > 1$, The system has slower response, no overshoot, and no oscillations.

Enhanced Bang-Bang Algorithm application

We suggest using this algorithm for first order systems and only critically damped and overdamped ($\zeta \geq 1$) second order systems. Undamped system may produce undesirable oscillations that may have unexpected behavior.

This solution has been tested in physical thermal heating and heating/cooling systems described in the [tools and prerequisites](#) section as the test equipment, and level control systems (Tested in industrial system not shown here) where we have inlet and outlet flow.

Enhanced Bang-Bang Algorithm theory of operation.

The block diagram for the enhanced Bang-Bang control algorithm is shown in Figure 4.

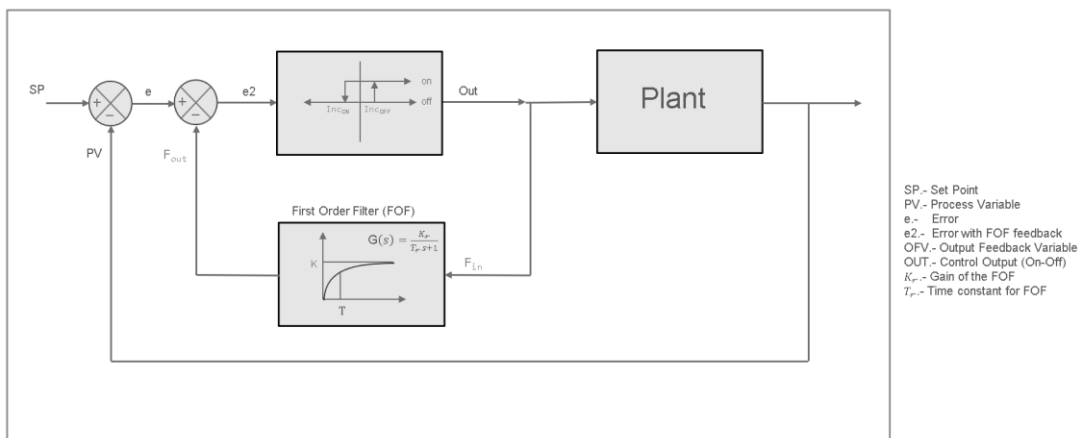
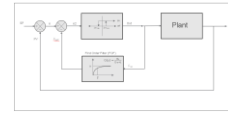


Figure 4. Enhanced Bang-Bang block diagram.



The bang-bang principle of operation is the on/off control with hysteresis, as the diagram shows the system will turn on when the input [e2] is greater than H but, it will hold on until [e2] is less than L. Figure 5 shows the block diagram of this section of the control.

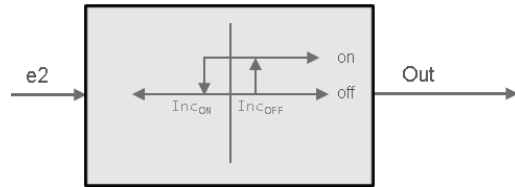


Figure 5. Bang-Bang

Normally this is all the bang-bang functionality, but we have added a feedback inner loop at the on/off output through a first order filter as shown in Figure 6. This filter is implemented mathematically in the algorithm.

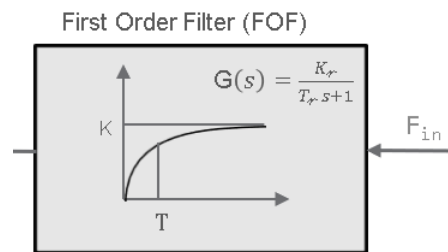


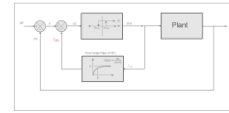
Figure 6. First Order filter at the feedback

This first order filter (FOF) will receive the status of the bang-bang (BB) (hysteresis) output block that is a 1 (one) or 0 (cero) depending if the output is on or off. The result will be a capacitance charge or discharge depending on the state of the Bang-Bang block output. The tendency of the FOF output will be K when the BB output is on and will tend to zero when the output is off.

The output of the FOF is subtracted of the error [e] producing a reduced [e2] that will tend to K, this means that when the error (e=SP-PV) is greater for enough time, e2 will tend to e-K_r, therefore e2 will be greater than H turning the output of the BB to on.

Because the output of the control is actuating the final control element that can be a relay to drive a heating resistor for an oven, a solenoid valve to let steam into the heat exchanger or an inlet valve recover the level of a tank, the plant will be also reducing the difference between the Setpoint [SP] and the Process Variable [PV].

The final control element will stay open until the plant reaches the difference stated by $e2 \leq L$ the output of the BB will turn off even when the plant has not yet reached the Setpoint, but then the feedback filter will begin a discharge provoking an increase on e2. The discharge will continue until e2 reaches H that will turn again the output of BB.



The process will continue to cycle between on/off until the PV reaches SP.

What is the enhancement of the Feedback First Order Filter?

The ultimate effect of the Feedback First Order filter in the Bang-Bang Control is to compensate for the dead time it takes between from the actuator that affects the measured variable and the sensor to report actual measurement. Let's take the heated tank example:

If we have the heater element in one side of the tank and the tank does not have an agitator to homogenize the tank temperature faster than convection currents, we have a dead time (t_0). This can make the bang-bang to overshoot from the set point and can be difficult to control with an On-OFF Control.

Another element that introduces a dead time into the system is the thermo-well of the sensing element, in some processes for example electroplating, the sensor needs to be in a thermo-well that is corrosion resistant such as nylamid. In this case thermo-well will introduce a dead time because thermal conductivity of the nylamid is less than the liquid that surrounds it.

With the feedback filter, the oscillation at the control output will begin earlier than if it only had the hysteresis comparator hence limiting the amount of heat deliver to the tank helping to avoid overshoot as the heated liquid arrives to the sensor.

Tunning the Bang-Bang.

Tunning method is quite intuitive. But is best to begin with small gain in the feedback filter and few units of error to turn on the control and few units to turn off the control. It can begin centered over cero. For example, start with [H = 0.5% of the control variable] and [L= - 0.5% of the control variable]. Make K=0 to see how the system reacts to a pure bang-bang.

The sample time should be equal to the periodic function call for the Bang-Bang function. This parameter is important because it will determine the system timing for the following steps.

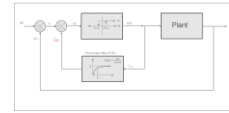
Check the overshoot after the system stabilizes, make [K] equal to overshoot and [Tao] equal to the dead time (t_0) to estimate this time (does not have to be precise) measure the time between the output of the actuator activates and when you can see a perceivable change of 0.5% in the control variable.

This will set up the Bang-Bang for the first pass tunning.

By observing the system capacity, you may reduce the gap between [H] and [L] to reduce magnitude of the fluctuations around the set point [SP].

You can also reduce or increase the on/off period by modifying [Tao] on the control. This will enhance the precision of the system output but will create and increase of on/off cycles in the actuator.

Be aware that if the actuator has a mechanical operation such as a relay, contactor or solenoid valve, the life of the actuator will be inverse of the number of on/off cycles, so you will need to make a trade off among life of the actuator and precision of the control.



Cooling Bang-Bang (Actuator to decrease the control variable)

The algorithm to decrease the control variable such as cooling in a heated tank or pressure release valve in a pressure tank is very similar to the heating diagram but with some changes as shown in figure 7.

Control variable decrease Bang-Bang Diagram

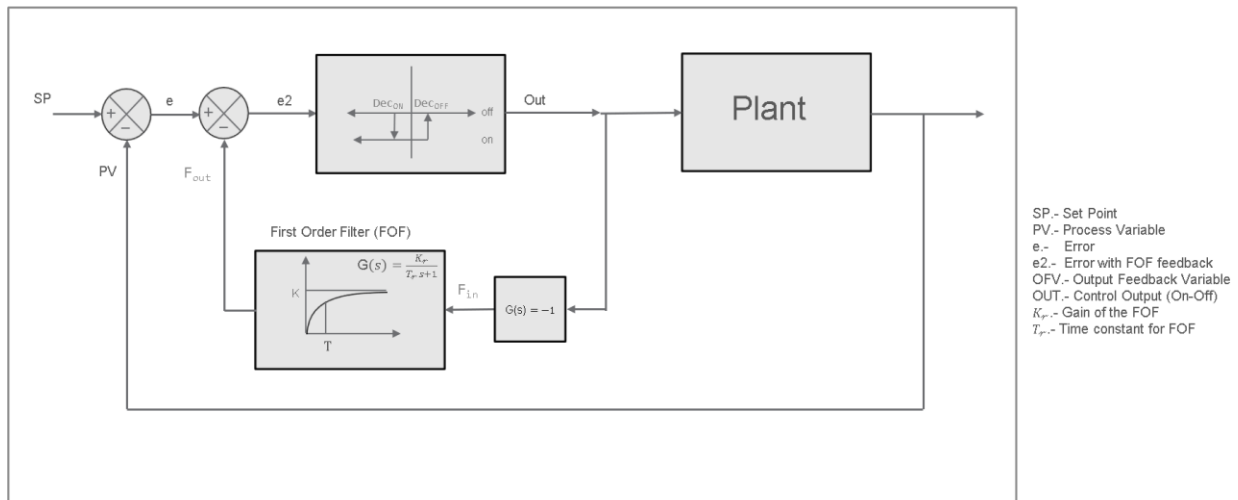


Figure 7. Bang-Bang where actuator decreases control variable.

In this case the output of the control will be a solenoid or a relay to actuate initiate the decrease of the variable, and example can be a valve to open cooling water for the system, an application for this type of system can be the cooling water for a heat exchanger to cool electronic equipment such as high-power rectifiers. Another application can be the cooling jacket of a reactor that reacts exothermally.

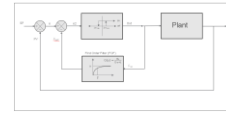
In many systems the control element is linear which helps to have a more precise control, but the solution is much costly.

The difference in the algorithm is that the decrease output is multiplied by -1 before feeding the input of the inner loop filter. The control different parameters, now the hysteresis turns on the decrease actuator when the e2 is less than de SP at Dec_{ON} point and will turn off the decrease actuator when the e2 is greater than Dec_{OFF} point.

Heating and cooling Bang-Bang

The last case for Bang-Bang is when you have both actuators for the same system, this is the case of application such as chrome plating or galvanizing where the systems need to be at a certain temperature to begin the process but once the process is in operation, the process generates more heat due to the electro plating current and hence needs to be cooled.

In this case we need to use the Bang-Bang in dual mode as shown in figure 8.



Control variable increase-decrease Bang-Bang Diagram

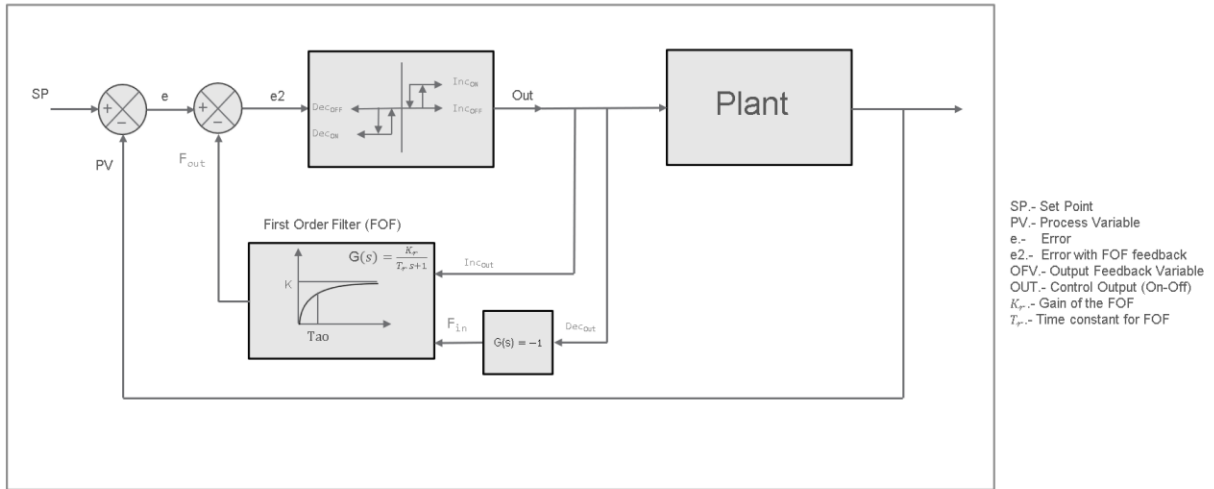


Figure 8. Bang-Bang where system has both type of actuators: Increase and Decrease

As you can see in figure 8, we have 2 hysteresis, one to drive the increase actuator and one to drive the decrease actuator. The key to tune this option is to make sure that the $[Dec_{ON}]$ parameter is always less than the $[Inc_{ON}]$ and is preferable that the off point of both parameters does not cross each other. Is preferable that both hysteresis are set up as mutually exclusive.

Bang-Bang programming

The programming of the Bang-Bang was done to handle Increase-Decrease and to turn on and off the whole controller.

Controller Structure.

The controller used for the testing was part of a ControlLogix performance demo with the I/O structure shown in figure 9.

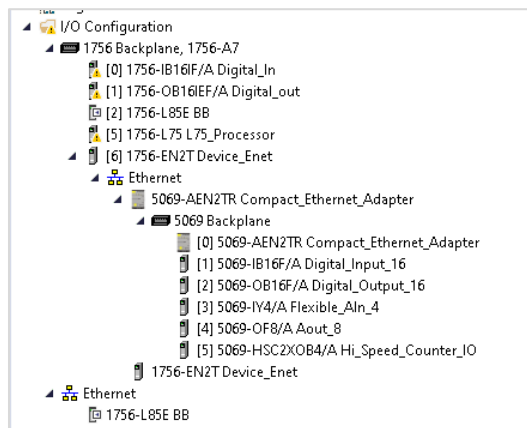
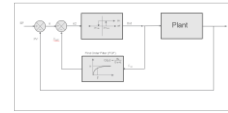


Figure 9. Controller I/O structure for testing



Inputs & Outputs for the testing system.

The input outputs used are:

- 10.1 PT100 RTD temperature sensor connected to Remote Compact I/O input in slot 3 input 0 (5069-IY4). Controller tag: *Compact_Ethernet_Adapter:3:I.Ch00.Data*.
- 11.2 DC output connected to 24 DC output card in Remote Compact I/O in slot 2 output 0 & 1. *Compact_Ethernet_Adapter:2:0.Pt00.Data* & *Compact_Ethernet_Adapter:2:0.Pt01.Data*.

Tasks.

The task that runs the Bang-Bang routine is a periodic task that for the purpose of this example and test has been set to 10ms seconds.

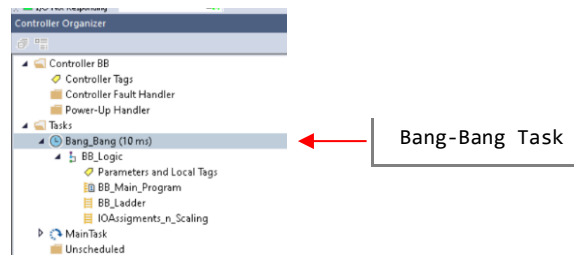


Figure 10. Bang-Bang Task

The Task has 3 sub-routines as shown in figure 10. The BB Main_Program has the call to the rest of the sub-routines which are:

- 12. BB_Ladder
- 13. I/O Assigments_n_Scaling

Figure 11 shows the call to these sub-routines in the main routine.

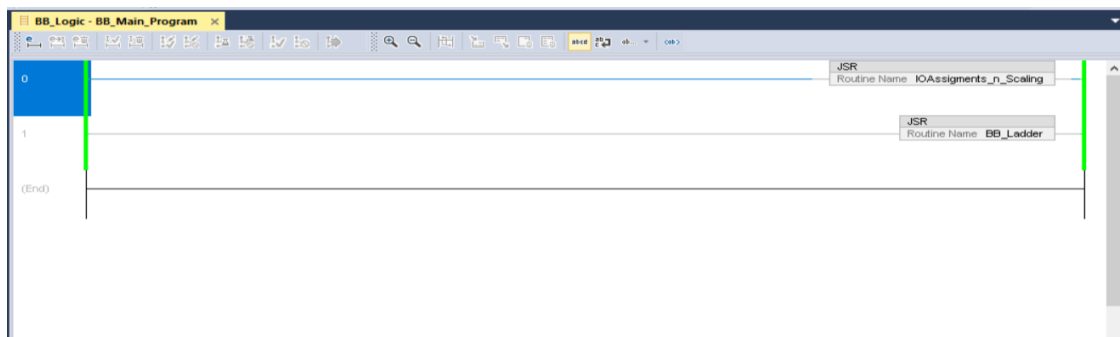


Figure 11. Bang-Bang Sub-routines calls.

Sub-routines

The {I/O Assigments_n_Scaling} routine scales analog input from the cardo and assigns the inputs to generic variables used in the main program, it also assigns the output from the {bb_Ladder} to Output card as shown in Figure 12.

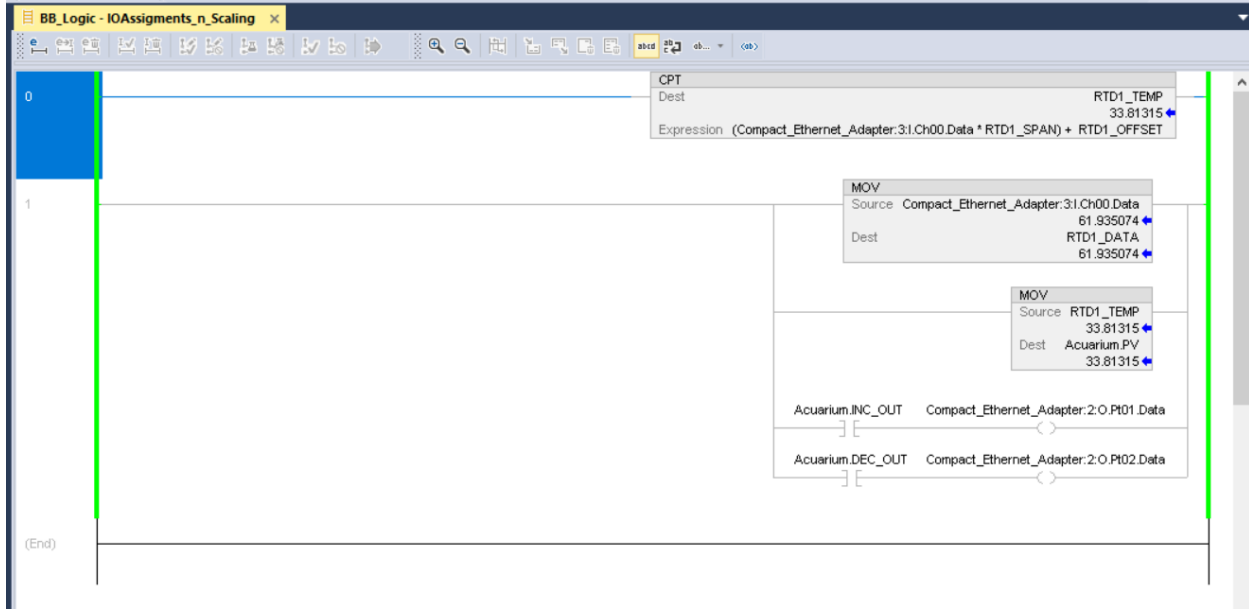
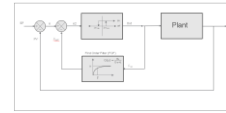


Figure 12. I/O Assignments and input scaling sub-routine

Routine {bb_Ladder} is a single rung that calls the Add on Instruction (AOI) created to run the Bang-Bang logic.

Since the program is an AOI, once included in the program, it can be used to control several systems and subsystems with a single instruction as scaling and assignments are provided for each system or subsystem.

The AOI call is illustrated in Figure 13.

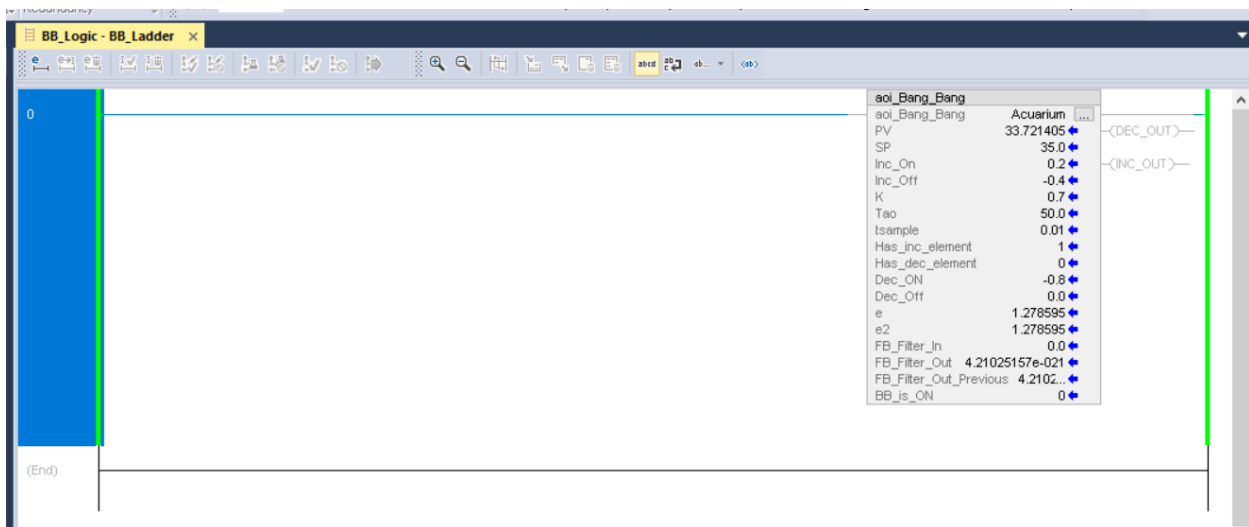
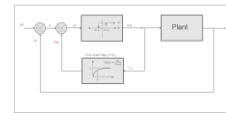


Figure 13. Add On Instruction (AOI) of Bang-Bang



Bang-Bang Add On Instruction (AOI).

The Bang-Bang Add On Instruction contains the instruction parameters, input variables and output variables to make the control work as well as the logic. The parameters that are input and output are shown in the faceplate made for Panelview Plus 7.

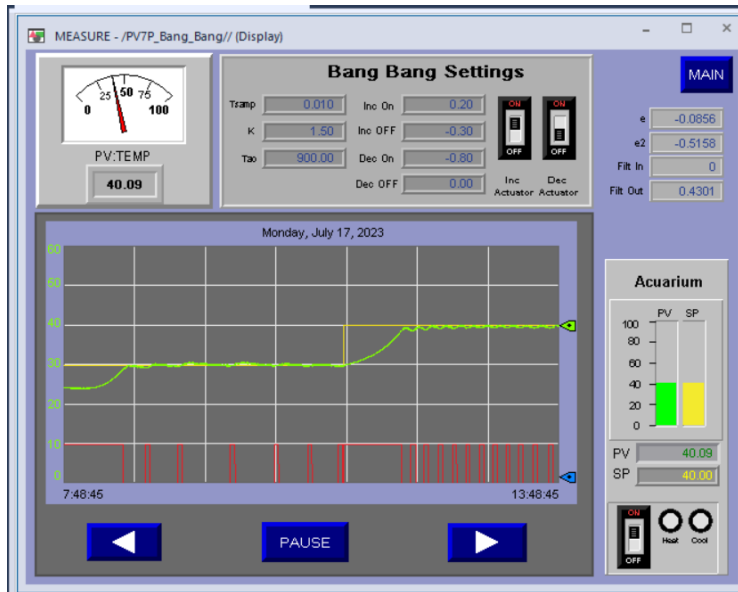


Figure 14. Input/Output Parameters for the Bang-Bang AOI

AOI Structure

The AOI instruction has a defined data type to name each control system by its unique name. In the case of this example the name of the system is “Acuarium” that has the {aoi_Bang_Bang} data type.

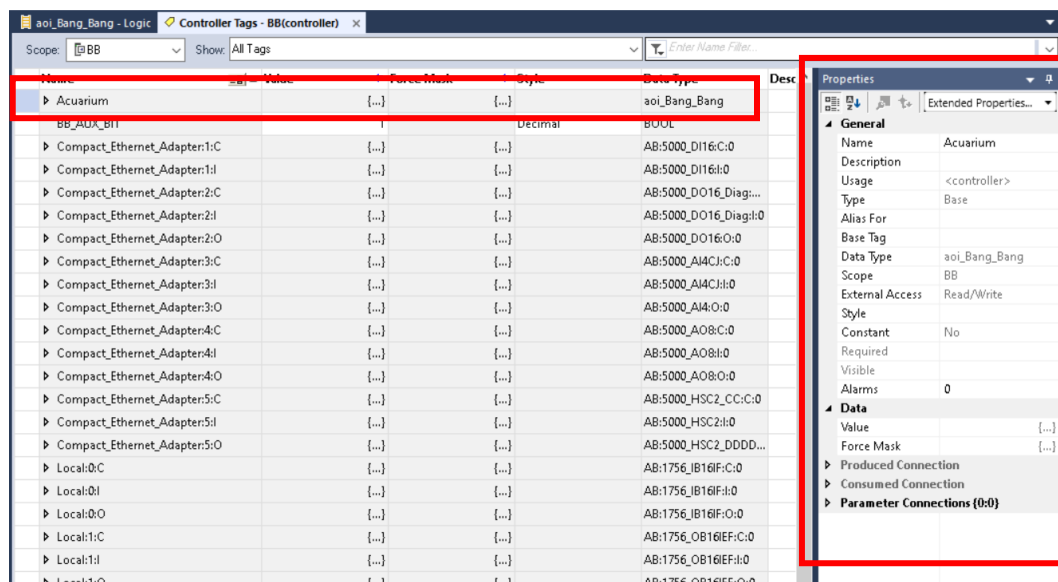


Figure 15. Variable Acuarium in Controller Tags with aoi_Bang_Bang Data Type

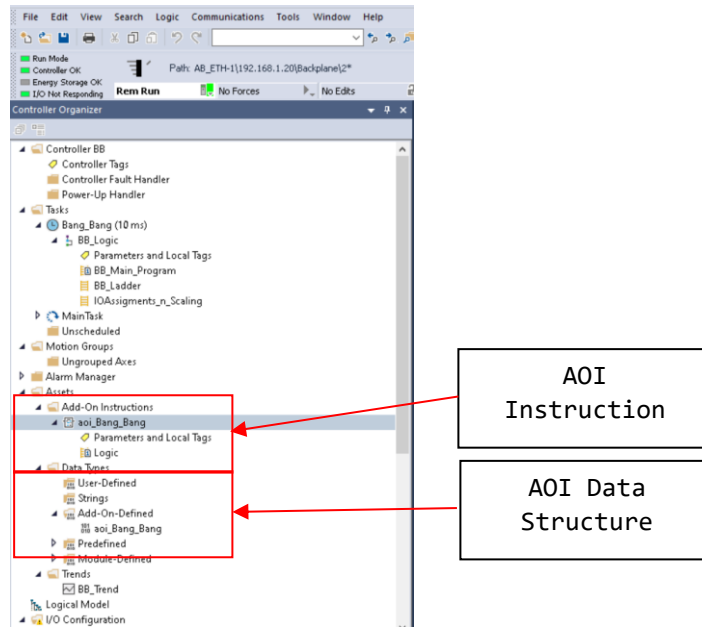
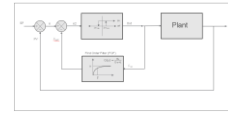


Figure 16. AOI Asset and AOI Data Type for Bang-Bang

Enable/Disable Parameters:

Parameter List and description.

[BB_is_ON] Boolean input variable to turn the control to ON or OFF.

[Has_inc_element] Boolean input to indicate if control has variable increase actuator.

[Has_dec_element] Boolean input to indicate if control has variable decrease actuator.

Operation parameters:

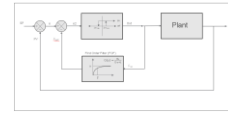
[PV] Process variable: This is a real floating-point parameter. You should assign the scaled variable of the input card to this variable.

[SP] Set Point: This is a real floating-point parameter. This variable will be set in the HMI or any input device that sets the reference for the control.

Calibration parameters:

[Inc_On] Real floating-point parameter. This is part of the hysteresis of the Bang-Bang that if the input error to the hysteresis greater than this value, the output to the increase the control variable is turned on.

[Inc_Off] Real floating-point parameter. This is part of the hysteresis of the Bang-Bang that if the input error to the hysteresis is less than this value, the output to the increase the control variable is turned off.



[Dec_On] Real floating-point parameter. This is part of the hysteresis of the Bang-Bang that if the input error to the hysteresis is less than this value, the output to the decrease the control variable is turned on.

[Dec_Off] Real floating-point parameter. This is part of the hysteresis of the Bang-Bang that if the input error to the hysteresis is greater than this value, the output to the decrease the control variable is turned off.

[tsample] Real floating-point parameter. This parameter should be equal to the time defined for the scan time of the periodic task for the Bang-Bang.

[Tao] Real floating-point parameter. This is the time constant in seconds for the first order filter at the inner loop feedback.

[K] Real floating-point parameter. This is the gain that the output of the first order system will tend after long period of time (normally 7 times Tao). If $K = 3$, then after 7 times Tao, the filter output will be near 3.

Monitoring Parameters

[e] Real floating-point variable. This indicates the difference between the setpoint and the process variable ($[e] = [SP] - [PV]$).

[e2] Real floating-point variable. Is the difference between the error [e] and the output of the first order filter [FB_Filter_Out].

[FB_Filter_In] Real floating-point variable. Is the input to the feedback filter which is the result of adding [INC_OUT] - [DEC_OUT] output parameters. These parameters are the actual outputs to actuator elements. Because [INC_OUT] and [DEC_OUT] parameters are Boolean, to add these parameters is required to use integer variables before assigning to the Filter input.

[FB_Filter_Out] Real floating-point variable. Is the output of the feedback filter which is the result of the digitalization of the transfer function of a first order system. For simplification purposes, the first order differential equation is transformed to digital sampling with Euler method.

The filter equation is as follows:

$$[Filter_Out] = \frac{[K] \cdot [Filter_In] + [Tao] * [Filter_Out_Previous]}{[Tao] + 1}$$

Output Parameters

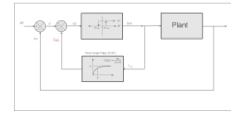
[INC_OUT] Boolean Output Parameter. This is the output that must be connected to the output card to drive the Increase control variable actuator.

[DEC_OUT] Boolean Output Parameter. This is the output that must be connected to the output card to drive the decrease control variable actuator.

AOI internal variables

The Add On Instruction has other internal variables required to execute the instruction such as conversion from Boolean to Integer. We will not describe each of

Simple On-Off Control for First Orders and Overdamped Systems



these variables in this document as the AOI instruction is open for reviewing and editing.

AOI programming

0

1

2

3

Tr = (Tao/Tsample)

$Ctr_Filter_Out = [(Filter_Gain * OFB + Filter_Time_Real * Ctr_Filter_Out_Previous) / (1 + Filter_Time_Real)]$

4

5

6

7

Block	Source A	Source B	Dest
SUB	SP	PV	e
SUB	e	FB_Filter_Out	e2
SUB	Inc_Out_TMP	Dec_Out_TMP	FB_Filter_In
DIV	Tao	tsample	Tao_Real
CPT			FB_Filter_Out

Expression $(K * FB_Filter_In + Tao_Real * FB_Filter_Out_Previous) / (1 + Tao_Real)$

4

5

6

7

INC_OUT

INC_OUT

DEC_OUT

DEC_OUT

Has_inc_element

Has_dec_element

BB_js_ON

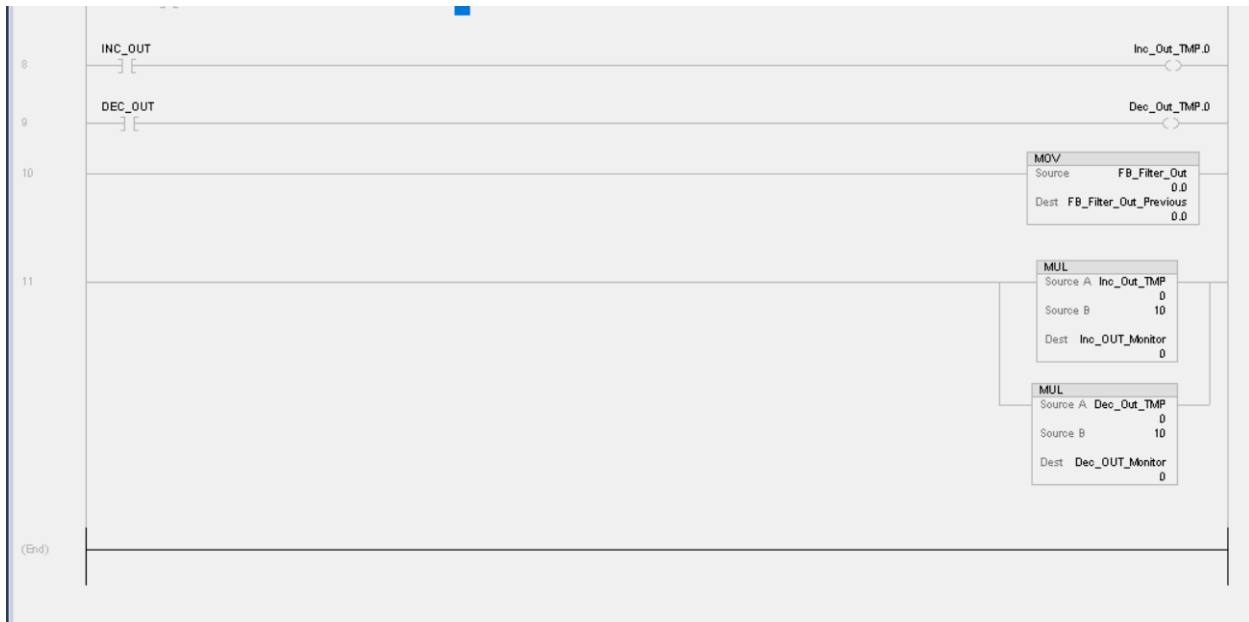
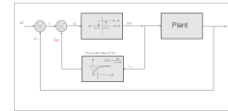
BB_js_ON

Has_inc_element

Has_dec_element

Block	Source A	Source B
GRT	e2	Inc_On
LES	Inc_On	Dec_On
LES	e2	Dec_On
GRT	Dec_Off	

Simple On-Off Control for First Orders and Overdamped Systems



Panelview plus 7 screens

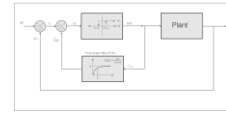
Panelview 7 machine edition screen is provided as face plate for the Bang-Bang Control.

The face plate is provided as a sample for a system and is included in the documentation package.

Panelview 7 Plus Performance faceplate

Faceplate

Tramp	0.010	Inc On	0.20
K	0.70	Inc OFF	-0.40
Tao	50.00	Dec On	-0.80
		Dec OFF	0.00



Implementation Steps

Studio 5000 AOI

To implement the Add On Instruction check the following steps.

1. Extract files from BB.ZIP into your working directory
2. Open file BB.acd into Studio 5000
3. Open the project where you want to use the Bang-Bang (it is assumed that the I/O mapping of your project is already done).
4. Highlight Select the aoi_Bang_Bang instruction under Assets menu in the controller organizer section of the Logix Designer.
5. Right click the mouse and select Copy as shown if Figure 17.
6. Go to the program you want to use the Bang-Bang and under Assets, highlight select the folder Add-On Instructions.
7. Verify that your target program has the new pasted AOI and under data type you should also have a new structure under Add-On-Defined.

Figure 17.
BB.acd
-
Select
copy
BB
AOI.

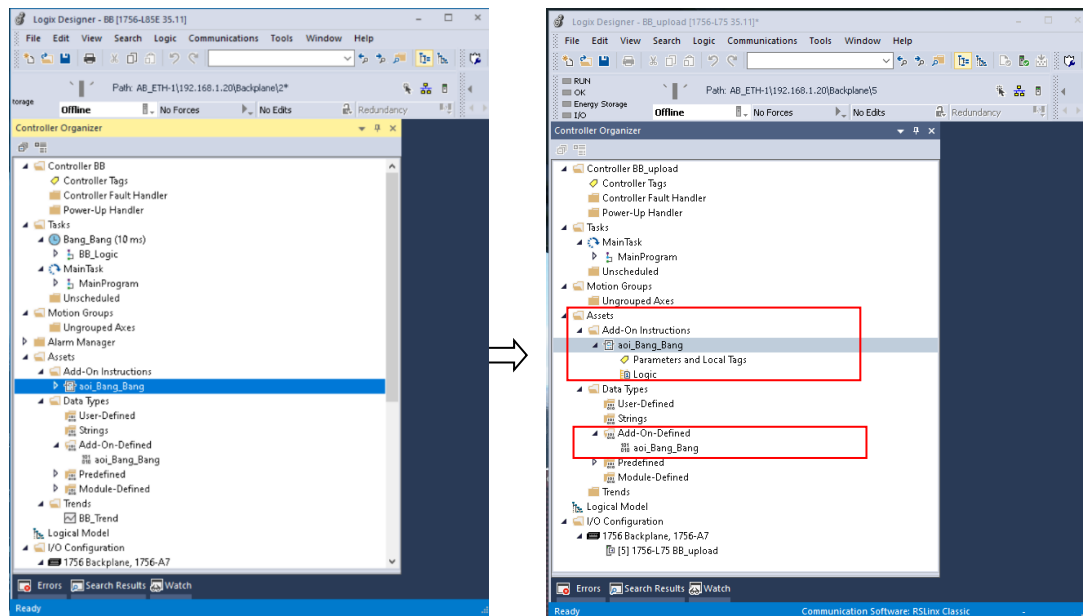
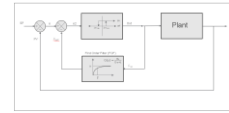


Figure 18. Paste AOI in target program.

8. Create a periodic task where you want to use the Bang-Bang Control or copy and paste the sample task from the BB.acd program. If you choose to copy the periodic task it must be done in 2 steps:
 - a. Select the Bang_Bang (10ms) Task, right click the mouse button and select copy.
 - b. Go to your target program and under Task folder right click select paste. The periodic task will be created in the target program.
 - c. From the BB.acd program under Bang_Bang (10ms) task right click select the BB_Logic routine and select copy.

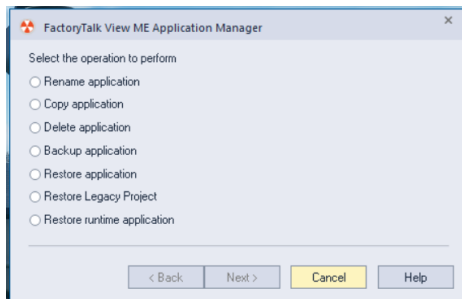


- d. In the target program select Bang_Bang (10ms) and right click to paste the logic.
9. Under Controller Tags define a new variable “Acuarium” (because this is the name of the system in the BB_Logic routine).
10. In the BB_Logic routine in the program named {IOAssignments_n_Scaling}, change the I/O Analog Input Address to match your project. Also change the Digital output to the Control Actuators to match your project.
11. Your Bang-Bang should be ready to work in your target program.

View Studio ME

To use the template for PanelView Plus 7 Performance, you will need to recover the project from the .mer file into the Studio 5000 View ME.

1. From the zip file unzip the file named PV7P_BB.mer (Remember this file is in version 12 for ViewME).
2. Use FactoryTalk ViewME Application Manager from the tools menu within the FactoryTalk ViewME application.



3. Select “Restore runtime application.”
4. Select the file BB.mer file.
5. Select Open application and the application should be restored.

You can also find many videos on how to restore a .mer application to recover